# Dataset Similarity to assess Semi-supervised Learning under Distribution Mismatch between the Labelled and Unlabelled Datasets

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Abstract—Semi-supervised deep learning (SSDL) is a popular strategy to leverage unlabelled data for training, when labelled data is not readily available. In real-world scenarios, different unlabelled data sources are usually available, with varying degrees of distribution mismatch, with respect to the labelled datasets. However, a quantitative and systematic approach to this selection problem would be preferable. It would enable the selection of unlabelled data for a given SSDL problem in a systematic way. In this work, we first test the SSDL MixMatch algorithm under various distribution mismatch configurations, to later propose a quantitative unlabelled dataset selection heuristic based on dataset dissimilarity measures. These are designed to systematically assess how distribution mismatch between the labelled and unlabelled datasets affects MixMatch performance. We refer to our proposed method as deep dataset dissimilarity measures (DeDiMs), designed to compare labelled and unlabelled datasets. They use the feature space of a generic Wide-ResNet and can be applied prior to learning, are quick to evaluate and model agnostic. The yielded strong correlation between MixMatch accuracy and the proposed DeDiMs in our tests, suggest a good fit for quantitatively ranking different unlabelled datasets ante hoc, according to expected MixMatch accuracy gain.

Impact Statement—Semi-supervised deep learning is an interesting alternative for training a deep learning model when few labelled observations are available, by leveraging unlabelled datasets. Different unlabelled data sources might be considered, bringing different distribution mismatch scenarios regarding the labelled dataset. In this work we assess the impact of distribution mismatch in training the semi-supervised MixMatch model, and propose a set of simple feature-space density dataset distances, referred to as deep dataset dissimilarity measures (DeDiMs). In our extensive test-bed, the evaluated DeDiMs yielded linear correlation coefficients of up to 96% to the MixMatch accuracy.

## Index Terms—Semi-supervised Deep Learning, MixMatch, Out

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#### I. INTRODUCTION

Training an effective deep learning solution typically requires a considerable amount of labelled data. In specific areas, like medical imaging technologies, high quality labelled data can be expensive to obtain, leading to a paucity of labelled data settings [4], [12]. Several approaches have been developed to address this data constraint, including data augmentation, transfer, weakly and semi-supervised learning, among others [32], [43]. Semi-supervised learning is an interesting approach for learning problems where little labelled data is available, or a range of labels is lacking. It leverages the use of unlabelled data which is often cheap to obtain [41]. Formally, in a semi-supervised setting both labelled and unlabelled datasets are used. Labelled observations  $X_l = \{x_1, \dots, x_{n_l}\}$  and their corresponding labels  $Y_l = \{y_1, \dots, y_{n_l}\}$  make up the labelled dataset  $S_l$ . The set of unlabelled observations is represented as  $X_u = \{x_1, \dots, x_{n_u}\}$ , therefore  $S_u = X_u$ . Semisupervised deep learning (SSDL) approaches can be grouped into pre-training [14], self-training or pseudo-labelled [15] and regularization-based. Regularization techniques include generative based approaches, along consistency loss term and graph based regularization [12]. A detailed survey on semisupervised learning can be found in [41].

The practical implementation of SSDL techniques in different contexts has been, however, limited; even considering its relative success in the real-world scenarios it has been leveraged in thus far [30]. As with other learning paradigms, the transfer of SSDL techniques from lab to real-world is complicated by violations of Independent and Identically Distributed (IID) assumptions. In principle, we would like to exploit available unlabelled data as flexibly as possible. In practice, mismatches between the labelled and unlabelled data sets can lead to serious performance degradation [30].

In [30], the authors call for more systematic and meaningful evaluation of SSDL approaches. A class distribution mismatch between labelled and unlabelled data is among the most important practical short-comings noted by the authors. The following example extends this problem. We can train a Convolutional Neural Network (CNN) to classify between COVID-19 ill and healthy patients using chest X-ray images, as for example seen in [7]. The labelled dataset  $S_l$  can include

a limited number of observations for each class. However, the unlabelled dataset  $S_u$  can include observations of patients with other lung pathologies. These observations correspond to what is known as Out of Distribution (OOD) data [23], leading to a class distribution mismatch between the labelled and unlabelled datasets. It also can be referred to a IID assumption violation. This problem can potentially harm the performance of a SSDL solution [30].

It begs the question how we can systematically select labelled and unlabelled data in non-IID settings such that performance on the downstream task is increased. A common recourse are what we call semantic matching heuristics, e.g., Tiny ImageNet (TI) supposedly is more similar to Canadian Institute for Advanced Research dataset of 10 classes (CIFAR-10) than to Modified National Institute of Standards and Technology dataset (MNIST), Street View House Numbers dataset (SVHN) more similar to MNIST than to ImageNet and so on. Practices of semantic matching can be traced to other fields of machine learning, too, including out-of-distribution detection [48] or the domain adaptation [46] literature. Insights from generative modelling should, at the very least, make us feel queasy about such an approach: a supposedly different data set like SVHN can have a higher likelihood under a generative model trained on ImageNet than ImageNet data itself [28].

## A. Problem statement

The central premise of this work is the quantitative impact assessment of class distribution mismatch between labelled and unlabelled data on SSDL. This notion stipulates that a mismatch negatively affects the accuracy of models trained with SSDL algorithms [30]. A mismatch occurs when the unlabelled data contains observations that do not correspond or are too dissimilar to the observations of any of the classes present in the labelled data. It is not clear though what exactly the effect is when this mismatch occurs:

- Does it always harm the model accuracy in the context of SSDL?
- Does it help to use unlabelled data that is, supposedly, semantically more similar to the labelled data?
- Furthermore, if certain unlabelled datasets indeed harm accuracy of SSDL trained models, is there a reliable way to select the unlabelled data in an informed way ante-hoc?

In order to establish points of reference for what follows we adopt the definitions below. Given a dataset  $S_1$  emanating from the data generating process y = f(x), with  $y \in \mathcal{Y} := \{1, ..., K\}$  being a set of labels, and a second dataset  $S_2$  emanating from the data generating process y' = g(x), with  $y' \in \mathcal{Y}' := \{1, ..., K'\}$ , we say that

**Definition 1.** Inside of Distribution (IOD) data: Dataset  $S_2$  is IOD relative to dataset  $S_1$  if  $f(\mathbf{x}) = g(\mathbf{x})$ . In particular, we must have that  $\mathcal{Y} = \mathcal{Y}'$ .

**Definition 2.** OOD data: Dataset  $S_2$  is OOD relative to dataset  $S_1$  if  $f(x) \neq g(x)$ . In particular, we may have that  $\mathcal{Y} \neq \mathcal{Y}'$ .

**Definition 3.** Class distribution mismatch in SSDL: A class distribution mismatch occurs if the unlabelled data  $S_u$  used for SSDL is OOD relative to the labelled data  $S_l$ .

In practice, f(x) and g(x) are typically not known explicitly. Thus, given two datasets  $S_1$  and  $S_2$  a definite formal verification of the class distribution mismatch property is not possible. Instead, it is usually assumed that two different datasets, e.g., CIFAR-10 and MNIST, derive from different data generative processes. This working definition of OOD data follows the existing literature on class distribution mismatch in SSDL [30] as well as OOD detection in deep learning [35]. We adopt this working definition for the OOD scenarios of our test bed. Note that different degrees of OOD contamination for  $S_u$  are possible as we describe in Section IV-A.

#### B. Contribution

In order to address the questions outlined in Section I-A we present a set of Deep Dataset Dissimilarity Measure (DeDiM)s to pre-assess the effectiveness of using an unlabelled dataset to use with MixMatch [5]. In <sup>1</sup> all code and experimental scripts, with automatic download of test bed data for ease of reproduction, can be found at. It entails the following contributions:

- We present and make available a comprehensive simulation sandbox, called non-IID-SSDL, for stress testing SSDL algorithms under various non-IID (distribution mismatch) configurations. We demonstrate that including OOD data in the unlabelled training dataset for the Mix-Match algorithm can yield different degrees of accuracy degradation compared to the exclusive use of IOD data. However, in most cases, using unlabelled data with OOD contamination still improves the results when compared to the default fully supervised configuration.
- Markedly, unlabeled that is supposedly semantically similar to the IOD labelled data does not always lead to the highest accuracy gain. This counter-intuitive result is very important, as it suggests that using semantically similar unlabelled datasets does not always yield the best accuracy gain for SSDL.
- We propose and evaluate four DeDiMs that can be used to rank unlabelled data according to the expected accuracy gain *prior* to SSDL training. They are cheap to compute and model agnostic, which make them amenable for practical application.
- Our test results reveal a strong correlation between the tested DeDiMs and MixMatch accuracy, making them useful for unlabelled dataset selection. Therefore, we propose the usage of the tested DeDiMs to select the unlabelled dataset for improved MixMatch accuracy. The best performing DeDiMs use a non-parametric density function approximation of the feature space, which results in an intriguing approach, to quantitatively describe the distribution mismatch between two datasets.

## II. RELATED WORK

In this work we address a combination of three overlapping problems that are often dealt separately in the literature: OOD detection, class distribution mismatch in SSDL, and dataset dissimilarity measures.

<sup>1</sup>https://gitlab.com/saul1917/mixmatch\_with\_ood.git

### A. OOD data detection

In the context of machine learning, OOD data detection refers to the general problem of detecting observations that belong to a data distribution different from the distribution of the training data [18]. OOD detection can be considered as a generalization of outlier detection, since it considers individual and collective outliers [37]. Further variations of the OOD data detection problem are novel and anomaly data detection [31], with different applications such as rare event detection and artificial intelligence safety [17], [1]. Classical OOD and anomaly detection methods rely on density estimation, e.g., Gaussian Mixture Models [24], robust moment estimation, like the Minimum Covariance Determinant method [36], prototyping, e.g., k-nearest neighbor algorithm [24], as well as kernel based variants such as Support Vector Data Description [40]. Also, a variety of neural network based approaches for novelty detection can be found [24], with a more data-oriented approach.

With the success of deep learning, recent works have addressed the generic problem of discriminative detection of OOD data for deep learning architectures. In general, discriminative OOD detectors can be categorized in outputand feature-based. For instance, a simple output based OOD detection approach was proposed in [19]. The authors framed OOD detection as a prediction confidence estimation problem. The proposed method relies on the Softmax output, sampling the maximum value. [23] introduced OOD data detection in neural networks using input perturbations. A temperature coefficient T in the calculation of the Softmax output and calibrated decision threshold  $\delta$  for OOD data detection.

More recently, in [22] authors argue that deep networks with Softmax output layers are over-confident for inputs dissimilar from the training data and hence propose the usage of the Mahalanobis distance in latent space. Similarly [38] also exploit latent representations, defining what they refer to as learning certificates: neural networks that map feature vectors to zero for IOD data. A more challenging OOD detection setting was tested, where half of each tested dataset is used as IOD data, and the other half is used as OOD data, making OOD detection harder. [48] proposes an OOD detector using the feature space as well. The approach fits different parametric distributions in the feature space of the data. The decision to discriminate between OOD and IOD data is done based on the estimation of the approximated parametric model. Unfortunately, no comparison with other popular OOD methods was presented. A similar approach with a simpler linear model trained with the statistical moments of the feature space can be found in [33].

In this concise overview of OOD detection methods, two different main categories for OOD detection can be found: output and feature space based. Moreover, we can see how dataset selection for bench-marking OOD detection is not quantitatively assessed, making the comparison of the algorithms harder. The datasets selected to bench-mark the methods are usually different for each work, and no prior quantitative evaluation of the difficulty of performing OOD detection is done.

### B. Class distribution mismatch in SSDL

The distribution mismatch between  $S_u$  and  $S_l$  is also referred as the identically and indepently distributed (iid) assumption violation. Different causes for this distribution mismatch can be distinguished, as discussed in [20]. We summarize them as

- Prior probability shift: The density of the targets in  $S_l$ is different to the real target densities in  $S_u$  (increasing the possibility of sampling noise). Class imbalance in the labelled dataset  $S_l$  is a special case of this setting, as discussed in [8].
- Covariate shift: The labelled dataset  $S_l$  might sample a different density of the features when compared to the unlabelled dataset  $S_u$ , causing a distribution mismatch between the two datasets. For example, for handwritten digit recognition, the sample of  $S_l$  might capture different stroke widths, when compared to  $S_u$
- Concept drift: For a same class or label, the features might change in the unlabelled dataset  $S_u$  when compared to the dataset  $S_l$ . For example, in the context of digit recognition, the dataset  $S_u$  might be a sample of digits painted in walls and doors in dark lighting conditions, and  $S_l$  can correspond to handwritten digits.
- Concept shift: It corresponds to a label change for a similar set of features. For instance, for sentiment analysis in audio, an observation might have different labels depending of the labeler (this is also related to label noise). In the context of distribution mismatch between  $S_l$ and  $S_u$ , as no label information is used from  $S_u$  during training.

In this work, we analyze the impact of distribution mismatch between  $S_l$  and  $S_u$  caused by a concept drift, as a mild distribution mismatch cause (for instance using SVHN as  $S_u$ and MNIST as  $S_l$ ). To create more significant distribution mismatch settings, we contaminate the unlabelled dataset  $S_u$ with different percentages of observations from completely different datasets (with different labels and features). For example, using MNIST as  $S_l$  and 50% of Gaussian Noise (GN) images with the remaining 50% of images from the MNIST dataset in Su.

As previously highlighted, in [30] the authors call for the need of a more extensive testing of SSDL techniques in realworld testing scenarios. One of them is the possible data distribution mismatch between the labelled and unlabelled training data. Real Mix was proposed [27] as a response to this, implementing a masking coefficient to OOD data for the unlabelled dataset. The masking coefficient is used as a threshold of the Softmax output of the model, discarding unlabelled data used only in the unsupervised term. The authors performed limited testing on the significance of using OOD unlabelled data, with relatively few OOD contamination scenarios tested. The OOD dataset consisted of the splitted CIFAR-10 dataset, in two halves with different semantics. A total of four levels of OOD contamination were tested. We argue for the need of testing different OOD datasets to more meaningfully understand their impact on SSDL.

More recently, the work in [10] proposes a simple approach

to deal with OOD data, by using soft labels averaged by the output of the model along a number of epochs. The evaluation includes a benchmark with different proportions of class distribution mismatch. The results yielded demonstrate an improved accuracy of the proposed method over other state of the art SSDL approaches when dealing with OOD data in the unlabelled dataset. However, MixMatch is not among the compared approaches. Moreover, the distribution mismatch scenarios were not extensive, testing only different degrees of mismatch contamination, and not evaluating the impact of different OOD data sources.

In [47] a SSDL robust framework to OOD data was proposed. Authors claim how OOD data far away from the decision boundaries affect less the SSDL performance than OOD data lying very close to the decision boundaries. However, we consider that testing around this very limited, as no explicit quantitative measure of distribution similarity was used. Authors also noted a high influence of data bach-normalization, where normalizing the data using far away OOD data can impact the accuracy of the model, more considerably. To address this issue, the authors proposed a dynamic approach to re-weight the observations in both batch-normalization and training time, using a gradient optimization approach for both. The model was tested using virtual adversarial training and the  $\Pi$  model, excluding the usage of MixMatch. The experiments included different degrees of OOD contamination and unlabelled datasets, however no comparison to other approaches explicitly designed for SSDL with OOD robustness was performed.

In [11] another approach for robustness SSDL was proposed, following also a per observation re-weighting approach, giving less weight to the observations that are most likely OOD. To calculate the per-observation weights, an uncertainty inspired approach as in [16] was implemented, using an ensemble of models yielded during the past epochs. The model was tested with the CIFAR-10 dataset (6-classes) with a varying degree of OOD contamination (the 4 classes left from CIFAR-10). No other unlabelled contamination data-sources were used. Unlike such previously commented work on SSDL robustness using unlabelled data with OOD observations, in this work we aim to quantify the notion of OOD data, correlating it with the SSDL accuracy using different unlabelled datasets with varying OOD degrees of contamination and data-sources. We consider that this analysis has been omitted in previous work. This quantification can be used to select an unlabelled dataset from another one, in a pre-hoc manner, without the need of training a model. This also allows us to analyze more the influence of OOD data, and quantitatively evaluate the OOD test beds for SSDL. Finally, the proposed method can be extended to weight how harmful can an unlabelled observation be for SSDL, making usage of the feature distribution to increase SSDL robustness between  $S_u$  and  $S_l$ . Using the feature distribution to this end, has not been fully explored in previous work.

## C. Dataset dissimilarity measures

The need of comparing two datasets, in this case the labelled  $S_l$  and unlabelled datasets  $S_u$  to quantify the prior data

mismatch between them leads us to the definition of dataset comparison measures. Computing a notion of dissimilarity between two sets of points (known as shape matching [25]) is typically more computationally expensive than calculating the dissimilarity between a set of points and another single point. Strategies to reduce this burden are primarily centered around enriching the object space with a probability measure which helps guide attention to important areas of comparison [25]. When starting with raw datasets, as is typically the case when trying to decide which data to use for SSDL, additional preprocessing or modelling steps would be necessary. Methods explicitly designed to compute dissimilarities between raw datasets for deep learning are, to the best of our knowledge, rare. In [39] authors define a dissimilarity measure based on the Euclidean distance between the frequency of a given feature function on two datasets, referred as the constrained measure distance. The calculation of the proposed measure can be efficiently performed through the usage of the covariance matrix of the feature function in the dataset.

More recently, authors in [6] proposed a distance dissimilarity index based on the statistical significance difference of the distance distributions between the two datasets. To calculate it, each data point in the test set is matched with the training data. After exchanging the associated observations, changes in the topology are assessed, using the distance distribution. The confidence p-value of the difference between the two distributions is calculated and used as a dissimilarity measure.

Note that our requirements differ from the above OOD detection and dissimilarity measure methods: we are interested in computationally cheap, retroactive and agnostic quantification of the OOD degree between two datasets. Approaches that are computationally expensive or retrospective, applied after the model has been trained, are not feasible to address class distribution mismatch before SSDL training. Closest to our work are the OOD detection ideas developed by [35]. The authors present introductory experiments on the correlation between OOD detection and the dataset dissimilarity using a genome distance [34]. We explore a similar comparison: the relationship between SSDL accuracy and OOD-IOD dissimilarity, which can be useful for a prior evaluation of unlabelled datasets for SSDL. This enables an interesting quantitative insight on the real impact of OOD data to SSDL accuracy, which we explore in this work.

## III. PROPOSED METHOD

Our approach is based on a simple idea: if OOD data indeed affects MixMatch SSDL accuracy we would like to be able to select the unlabelled data *prior* to SSDL such that resulting test accuracy of the model is maximized. To that end we propose and evaluate a number of DeDiMs. They provide a quantitative notion of similarity between the inputs of the IOD labeled data and the inputs of the OOD unlabelled data. In this work we implement a set of DeDiMs based on dataset subsampling, as image datasets are usually large, following a sampling approach for comparing two populations, as seen in [21]. We compute the dissimilarity measures in the feature space of a generic Wide-ResNet pre-trained on

ImageNet, making our proposed approach non-specific to the SSDL model to be trained. This enables an evaluation of the unlabelled data before training the SSDL model. The proposed measures in this work are meant to be simple and quick to evaluate with practical use in mind. We propose and test the implementation of two Minkowski based distance sets,  $d_{\ell_2}\left(S_a, S_b, \tau, \mathcal{C}\right)$  and  $d_{\ell_1}\left(S_a, S_b, \tau, \mathcal{C}\right)$ , corresponding to the Euclidean and Manhattan distances, respectively, between two datasets  $S_a$  and  $S_b$ . Additionally, we implement and test two non-parametric density based dataset divergence measures; Jensen-Shannon  $(d_{JS})$  and cosine distance  $(d_C)$ . For all the proposed dissimilarity measures, the parameter  $\tau$  defines the sub-sample size used to compute the dissimilarity between the two datasets  $S_a$  and  $S_b$ , and C the total number of samples to compute the mean sampled dissimilarity measure. The general procedure for all the implemented distances is detailed as follows.

- We randomly sub-sample each one of the datasets  $S_a$  and  $S_b$ , with a sample size of  $\tau$ , creating the sampled datasets  $S_{a,\tau}$  and  $S_{b,\tau}$ .
- We transform an input observation  $x_i \in S_i$ , with  $x_i \in$  $\mathbb{R}^n$ , being n the dimensionality of the input space, using the feature extractor f, yielding the feature vector  $h_i$  =  $f(\boldsymbol{x}_i)$ .
- The feature vector  $\boldsymbol{h}_i \in \mathbb{R}^{n'}$  has dimension n' dimensions, with n' < n. For instance, the implemented feature extractor f uses the ImageNet pretrained Wide-ResNet architecture, extracting n' = 512 features. This yields the two feature sets  $H_{a,\tau}$  and  $H_{b,\tau}$ .

For the Minkowski based distance sets  $d_{\ell_2}(S_a, S_b, \tau, \mathcal{C})$ ,  $d_{\ell_1}(S_a, S_b, \tau, \mathcal{C})$ , we perform the following steps for the sets of features obtained in the previous description  $H_{a,\tau}$  and  $H_{b,\tau}$ :

- For each feature vector  $h_j \in H_{a,\tau}$ , find the closest feature vector  $h_k \in H_{b,\tau}$ , using the  $\ell_p$  distance, with p = 1 or p = 2 for the Manhattan and Euclidean distances, respectively:  $d_j = \min_k \|\boldsymbol{h}_j - \boldsymbol{h}_k\|_n$ . We do this for a number of C samples, yielding a list of distance  $\text{calculations } d_{\ell_p}\left(S_a, S_b, \tau, \mathcal{C}\right) = \Big\{\widehat{d}_1, \widehat{d}_2, ..., \widehat{d}_{\mathcal{C}}\Big\}.$
- We compute a reference list of distances for the same list of samples of the dataset  $S_a$  to itself (intra-dataset distance), thereby computing  $d_{\ell_p}(S_a, S_a, \tau, \mathcal{C})$ . This yields a list of reference distances  $d_1, d_2, ..., d_C$ . In our case  $S_a$ corresponds to the labelled dataset  $S_l$ , as the distance to different unlabelled datasets  $S_u$  is to be computed. We highlight that this should result in values close to zero. However, as different samples are used for each distance computation, the results are not exactly zero.
- To ensure that the absolute differences between the reference and inter-dataset distances  $d_c = |\vec{d_c} - \vec{d_c}|$  are statistically significant, we compute the p-value associated with a Wilcoxon test.
- After the distance set between two datasets  $d_{\ell_n}(S_a, S_b, \tau, \mathcal{C})$  is obtained, its average reference subtracted distance  $\overline{d}$  and its corresponding statistical significance p-value are computed.

As for the density based distances implemented we follow a similar sub-sampling approach, with these steps:

- For each dimension r = 1, ..., n' in the feature space, we compute the normalized histograms to approximate the density functions  $p_{r,a}$ , in the sample  $H_{a,\tau}$ . Similarly, we compute the normalized histograms to yield the set of approximate density functions  $p_{r,b}$  for r = 1, ..., n', using the observations in the sample  $H_{b,\tau}$ .
- For the Jensen-Shannon divergence  $(d_{IS})$  and the cosine distance  $(d_C)$ , we compute the sum of the dissimilarities between the density functions  $p_{r,a}$  and  $p_{r,b}$ , to yield the estimated dissimilarity for the sample j:  $\hat{d}_j =$  $\sum_{r=1}^{n'} \delta_g(p_{r,a}, p_{r,b})$ , where g = JS and g = C for the Jensen-Shannon divergence and the cosine distance, respectively. We do this for all the C samples, yielding the list of inter-dataset distances:  $d_1, d_2, ..., d_{\mathcal{C}}$ . To lower the computational burden, we assume that the dimensions are statistically independent. This assumption also simplifies the likelihood calculation, as seen in several likelihoodbased machine learning algorithms.
- Similar to the Minkowski distances, we compute the intradataset distances for the dataset  $S_a$ , in this context the labelled dataset  $S_l$ , to obtain the list of reference distances  $d_1, d_2, ..., d_C$ .
- Similarly, to verify that the inter- and intra-dataset distance differences  $d_c = |\hat{d_c} - \check{d_c}|$  are statistically significant, we compute the p-value associated with a Wilcoxon test. The distance computation yields the sample mean distance d and its statistical significance p-value.

The proposed dissimilarity measures do not fulfill the conditions to be a mathematical metric or pseudo-metric since the distance of an object to itself is not strictly zero (but tends to be close) and symmetry properties are not fulfilled for the sake of evaluation speed [13]. Despite these relaxations, we will see that these dissimilarity measures, especially the two that are density based, are an effective proxy for estimating the  $S_{u,OOD}$  accuracy gain.

To quantitatively measure how related the distances between  $S_l$  and  $S_u$  and the yielded SSDL accuracy are, we calculate the Pearson coefficient between the distance measures and the SSDL accuracy. This verifies the linear correlation between them. Table IV describes the Pearson coefficient for each implemented dissimilarity measure and each SSDL configuration.

In summary, we propose to quantitatively rank a set of candidate unlabelled datasets  $S_{u,1}, S_{u,2}, ..., S_{u,k}$  according to a dissimilarity measure  $d(S_l, S_u)$ , instead of using quantitative based heuristics. In all the tests of this work, we used n' = 512,  $\tau = 80$  and  $\mathcal{C} = 10$ .

## IV. EXPERIMENTS

# A. Semi-supervised Deep Learning setup

The basis for all SSDL experiments in this paper is the MixMatch algorithm, a state of the art SSDL method [5]. MixMatch estimates pseudo-labels for unlabelled data  $X_u$ , and also implements an unsupervised regularization term. Pseudolabel  $\hat{y}_i$  estimation is performed with the average model output of a transformed input  $x_i$ , with K number of different transformations. The pseudo-labels  $\hat{y}$  are further sharpened with a temperature parameter  $\rho$ . To further augment the data using

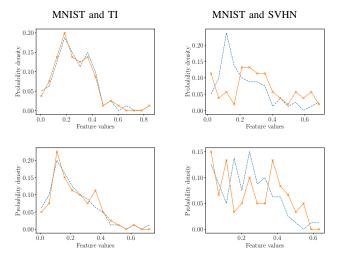


TABLE I
FEATURE DISTRIBUTION FOR A MODEL TRAINED WITH MNIST LABELLED DATA (CONTINOUS ORANGE LINE IN BOTH PLOTS), AND TI AND SVHN UNLABELLED DATA (LEFT AND RIGHT COLUMN, RESPECTIVELY, BLUE DASHED LINE IN BOTH). FOR EACH PLOT A DIFFERENT DATASET PARTITION WAS USED. FROM TOP TO BOTTOM, FOR EACH ROW: FEATURE 372 AND 159.

both labelled and unlabelled samples, MixMatch makes use of the MixUp algorithm by [45] which builds linear interpolations between labelled and unlabelled observations. For supervised and semi-supervised loss functions, the cross-entropy and the Euclidean distance, are used, respectively. The regularization coefficient  $\gamma$  controls the direct influence on unlabelled data. Unlabelled data also influences the labelled data term since unlabelled data is used also to artificially augment the dataset with the Mix Up algorithm. This loss term is used at training time, for testing, a regular cross entropy loss is implemented. For a detailed description of the MixMatch algorithm we refer to [5]. We use the recommended hyperparameters documented in the supplementary material.

# B. SSDL with OOD data ablation test bed

To assess the effect of OOD unlabelled data  $S_u$  on the accuracy of SSDL models trained with MixMatch, we construct an ablation non-IID-SSDL sandbox, with five variables: (1) base data  $S_{\text{IOD}}$  which constitutes the original task to be learned, (2) the type of OOD data  $T_{\text{OOD}}$ , with the OOD data source  $S_{\text{u,OOD}}$ , (3) the relative amount of OOD data among the unlabelled data  $\%_{\text{u,OOD}}$ , (4) and the amount  $n_l$  of labelled observations. Each of the four axes is explored by varying only one of the variables at a time while keeping the others constant. This allows us to isolate the effect of the individual variables. We consider three configurations for  $S_{\text{IOD}}$  comprising MNIST,CIFAR-10 and FashionMNIST. A total of three configurations for  $T_{\text{OOD}}$ (Other-Half (OH), Similar (Sim) and Different (Dif)) are tested. We derived the possible types of OOD data from the existing literature cited in Section II. In the OH setting half of the classes and associated inputs are taken to be the  $S_{\text{IOD}}$  data whereas the other half of classes are taken to be the  $S_{\rm u,OOD}$  data. Similar is a  $S_{u,OOD}$  dataset that is assumed to be semantically related to  $S_{IOD}$ , e.g., MNIST and SVHN. Different is a  $S_{u,OOD}$ 

dataset that is supposedly semantically unrelated to  $S_{\rm IOD}$ , e.g., MNIST and TI. There are five configurations for  $S_{\rm u,OOD}$  as explained above: the other half OH, a similar dataset, and three different datasets including two noise baselines. They include SVHN, TI, GN, Salt and Pepper Noise (SAPN) and Fashion Product (FP). Please see Table II for the per task pairings. Each configuration represents a multi-class classification task with  $|\mathcal{Y}|=5$ , that is a random subset of half of the classes of base data  $S_{\rm IOD}$ .

We vary the relative amount of OOD data %u,OOD between 0, 50 and 100 as well as the amount of labelled datapoints  $n_l$ between 60, 100 and 150. We study the behaviour of MixMatch under very limited number of labels settings, where the benefit of SSDL is usually higher. This makes the impact of distribution mismatch more evident. Note that for each result entry you can see in Table II we performed ten experimental runs and report the accuracy mean and standard deviation of the models performing best on the test data from each run, as overfitting is very likely to happen with a low  $n_l$ . For each run we sampled a disjunct subset of data from  $S_{IOD}$  and  $S_{u,OOD}$  to obtain the required number of labelled  $n_l$  and unlabelled  $n_u$ samples for the run. Descriptive statistics (mean and standard deviation) for standardization of the neural networks inputs were only computed from these subsets to keep the simulation realistic and not use any information from the global training data. All other parameters (number of unlabelled observations  $n_u = 3000$ , neural network architecture, the set of optimization hyperparameters, number of training epochs) are kept constant across all experiments to enable direct comparison with respect to the variable parameters of the system. We clarify that the goal of this test-bed is to assess the impact of distribution mismatch for MixMatch, rather to achieve state of the art performance with MixMatch on the given data. Such hyperparameters are described in the supplementary material. Note that it is possible to extend the test bed to other effects of interest. We address some of these ideas in Section VI.

## C. Dissimilarity distance measurements

In Table III we show the dissimilarity results for the tested labelled and unlabelled dataset combinations. We tested the dissimilarity measures detailed in Section III, namely the Manhattan or  $\ell_1$  distance  $d_{\ell_1}$ , the Euclidean distance  $d_{\ell_2}$ , the cosine distance  $d_C$  and the Jensen-Shannon  $d_{\rm JS}$  divergence. The distances and divergences are computed without the need of choosing or training a model, making the proposed approach appealing to choose unlabelled datasets before even choosing any SSDL approach.

As a complementary quantitative test, in Table I we show the probability density function approximation plots of some of the features for the MNIST dataset, using both the similar dataset chosen (SVHN) and the different dataset selected (TI). We picked the features presenting the smallest divergences for the chosen datasets. The density functions were built using random samples for both data pairs. The probability density function approximation plots illustrate in a summarized manner the similarity computed between the two compared datasets, and its correlation with the measured Jensen-Shannon and cosine divergences.

TABLE II

Results for the class distribution mismatch experiment, best OOD performance in bold per configuration (mean  $\pm$  standard DEVIATION). EACH RESULT ENTRY IN THE TABLE REPRESENTS THE MEAN AND VARIANCE OF ACCURACY ACROSS TEN RANDOM EXPERIMENTAL RUNS PER ENTRY. FOR A DETAILED DESCRIPTION OF SYMBOLS AND THE EXPERIMENT SEE SECTION IV-B.

$\mathbf{S_{IOD}}$	$T_{\rm OOD}$	$S_{uOOD}$	%uOOD	60	100 n <sub>1</sub>	150	Row. no.
MNIST	Fully supervised baseline		$0.457 \pm 0.108$	$0.559 \pm 0.125$	$0.645 \pm 0.101$	0	
	SSDL baseline (no OOD data)			$0.704 \pm 0.096$	$0.781 \pm 0.065$	$0.831 \pm 0.062$	1
	ОН	OH-MNIST	50	$0.679 \pm 0.108$	$0.769 \pm 0.066$	$0.802 \pm 0.054$	2
			100	$0.642 \pm 0.111$	$0.746 \pm 0.094$	$0.798 \pm 0.070$	3
	Sim	SVHN	50	$0.637 \pm 0.098$	$0.745 \pm 0.081$	$0.801 \pm 0.069$	4
			100	$0.482 \pm 0.113$	$0.719 \pm 0.058$	$0.765 \pm 0.072$	5
		TI	50	$0.642 \pm 0.094$	$0.739 \pm 0.074$	$0.809 \pm 0.066$	6
~			100	$0.637 \pm 0.097$	$0.732 \pm 0.074$	$0.804 \pm 0.071$	7
	Dif	GN	50	$0.606 \pm 0.0989$	$0.713 \pm 0.087$	$0.786 \pm 0.065$	8
			100	$0.442 \pm 0.099$	$0.461 \pm 0.073$	$0.542 \pm 0.062$	9
		SAPN	50	$0.631 \pm 0.102$	$0.735 \pm 0.082$	$0.813 \pm 0.057$	
			100	$0.48 \pm 0.0951$	$0.524 \pm 0.09$	$0.563 \pm 0.095$	11
	Fully supervised baseline			$0.380 \pm 0.024$	$0.445 \pm 0.042$	$0.449 \pm 0.022$	12
	SS	DL baseline (no OOD		$0.453 \pm 0.046$	$0.474 \pm 0.019$	$0.501 \pm 0.033$	13
	OH	OH-CIFAR-10	50	$0.444 \pm 0.040$	$0.472 \pm 0.039$	$0.525 \pm 0.050$	14
	OH		100	$0.443 \pm 0.023$	$0.472 \pm 0.047$	$0.499 \pm 0.054$	15
2	Sim	TI	50	$0.435 \pm 0.054$	$0.473 \pm 0.039$	$0.543 \pm 0.040$	
CIFAR-10			100	$0.417 \pm 0.020$	$0.480 \pm 0.039$	$0.498 \pm 0.042$	17
≊	Dif	SVHN	50	$0.419 \pm 0.027$	$0.464 \pm 0.044$	$0.469 \pm 0.056$	18
ರ			100	$0.385 \pm 0.034$	$0.418 \pm 0.035$	$0.440 \pm 0.046$	19
		GN	50	$0.409 \pm 0.047$	$0.454 \pm 0.048$	$0.491 \pm 0.032$	20
			100	$0.297 \pm 0.029$	$0.306 \pm 0.034$	$0.302 \pm 0.038$	21
		SAPN	50	$0.438 \pm 0.029$	$0.455 \pm 0.037$	$0.485 \pm 0.034$	22
			100	$0.236 \pm 0.031$	$0.246 \pm 0.032$	$0.232 \pm 0.022$	23
	Fully supervised baseline		$0.571 \pm 0.073$	$0.704 \pm 0.066$	$0.720 \pm 0.093$	24	
	SSDL baseline (no OOD data)		$0.715 \pm 0.049$	$0.760 \pm 0.044$	$0.756 \pm 0.069$	25	
	ОН	OH-FashionMNIST	50	$0.714 \pm 0.049$	$0.721 \pm 0.104$	$0.765 \pm 0.053$	26
ST			100	$0.660 \pm 0.061$	$0.711 \pm 0.090$	$0.747 \pm 0.061$	27
FashionMNIST	Sim	FP	50	$0.707 \pm 0.039$	$0.724 \pm 0.030$	$0.778 \pm 0.078$	28
			100	$0.546 \pm 0.101$	$0.542 \pm 0.099$	$0.540 \pm 0.105$	29
<u>.</u>	Dif	ті	50	$0.690 \pm 0.065$	$0.745 \pm 0.093$	$0.792 \pm 0.058$	30
Shi			100	$0.690 \pm 0.073$	$0.728 \pm 0.066$	$0.794 \pm 0.056$	
꺒		GN	50	$0.644 \pm 0.061$	$0.689 \pm 0.075$	$0.755 \pm 0.055$	32
			100	$0.352 \pm 0.025$	$0.366 \pm 0.065$	$0.361 \pm 0.057$	33
		SAPN	50	$0.671 \pm 0.072$	$0.708 \pm 0.095$	$0.729 \pm 0.088$	34
			100	$0.276 \pm 0.069$	$0.297 \pm 0.046$	$0.283 \pm 0.059$	35

#### V. RESULTS

The experimental setup used in this work is detailed in the supplementary material. Table II shows the results of the distribution mismatch experiment described in Section IV-A. We make a number of observations. From the yielded results, we can observe in the majority of cases, how using IOD unlabelled data or a 50-50 mix of IOD and OOD unlabelled data beats the fully supervised baseline. For instance take the results in row 0 vs. the results yielded in rows 2-7 (for the SSDL model). A clear advantage of the SSDL model is revealed over the supervised model, even under distribution mismatch settings. The gains range from 15% to 25% for MNIST, 10% to 15% for CIFAR-10 and 7% to 13% for FashionMNIST across all  $S_{u,OOD}$  and  $n_l$ . As expected, in most of the cases the accuracy is degraded when including OOD data in  $S_u$ , with a more dramatic hit when noisy datasets (SAPN, GN) are used as OOD data contamination.

Another interesting observation from the yielded results is related to the semantic similarity and the measured distance between an unlabelled and labelled dataset, and the yielded SSDL accuracy using both datasets. A lower MixMatch accuracy can be yielded using an unlabelled dataset with less resemblance or semantically different dataset, when compared to using a more semantically similar unlabelled dataset. This is observed when  $S_l$  =CIFAR-10,  $n_l$  = 100 and  $n_l$  = 150, where OOD unlabelled data from TI (row 16) results in more accurate models than using the other half of CIFAR-10 as  $S_{u,OOD}$  (row 14). It is interesting that an  $S_{u,OOD}$  dataset of type different can be more beneficial than a  $S_{u,OOD}$  dataset of type *similar*. This is also the case for FashionMNIST and TI (row 31) versus FP at  $n_l = 150$  (row 29). This contradicts the common heuristic that unlabelled data that appears semantically more related to the labelled data is always the better choice for SSDL. Rather, as we demonstrate in the second set of results below, a notion

of distance in the feature space between labelled and unlabelled data offers a more consistent and quantifiable proxy for the expected benefit of different unlabelled datasets.

As for the qualitative test results, Table I shows the density functions approximated for randomly selected samples for the MNIST-TI and MNIST-SVHN dataset pairs. The plots reveal a stronger density based similarity between the MNIST and ImageNet than the MNIST and SVHN datasets. This in spite of the perhaps higher perceptual similarity of the SVHN dataset to the MNIST dataset (both represent numbers, the first one in natural scenes, and the second one in handwritten images). This correlates well with the quantitative figures yielded in Table III. For instance, in row 3, the MNIST dataset is more dissimilar to the SVHN dataset (MNIST contaminated by 100% with the SVHN dataset), than the TI dataset (MNIST contaminated by 100% with the TI dataset), revealed in row 5. This also highly correlates with the final SSDL accuracy yielded with both unlabelled datasets (MNIST contaminated by 100% with SVHN, in row 5, and TI, in row 7) shown in Table II. MixMatch shows a higher accuracy when using TI as an unlabelled dataset compared to using SVHN as unlabelled data.

The second set of results demonstrate the potential of using distance measures as a systematic and quantitative ranking heuristic when selecting unlabelled datasets for the MixMatch algorithm. The exact distances, as described in Section III, for all OOD configurations from the ablation study can be found in Table III. We can observe that these distances trace the accuracy results found in Table II, as confirmed by the Pearson correlation. This correlation is quantified in Table IV with the cosine based density measure  $d_c$  correlating particularly well with the accuracy results of Table II. Also, the p-values are consistently lower for the density based distances (with less p-values higher than 0.05, as seen in Table III), meaning that

TABLE III Distance measures between the labelled and unlabelled datasets  $S_l$  and  $S_u$  (mean  $\pm$  standard deviation). Numbers in Italics correspond to results with p>0.05 for the Wilcoxon test.

$\mathbf{S}_{\mathbf{l}}$	$\mathbf{S_u}$	$\%_{uOOD}$	$d_{\ell_2}$	$\mathbf{d}_{\ell_1}$	$d_{ m JS}$	$d_{\mathrm{C}}$	Row no.
MNIST	ОН	50	$0.011 \pm 0.006$	$0.459 \pm 0.28$	$0.266 \pm 0.221$	$0.811 \pm 0.512$	0
		100	$0.014 \pm 0.019$	$0.38 \pm 0.507$	$1.001 \pm 0.725$	$1.263 \pm 0.665$	1
	SVHN	50	$0.09 \pm 0.017$	$1.569 \pm 0.504$	$6.789 \pm 0.924$	$12.021 \pm 1.757$	2
		100	$0.25 \pm 0.053$	$4.702 \pm 1.04$	$52.349 \pm 3.292$	$42.026 \pm 4.311$	3
	TI	50	$0.008 \pm 0.023$	$1.519 \pm 0.223$	$3.663 \pm 0.772$	$5.512 \pm 0.767$	4
		100	$0.217 \pm 0.04$	$4.3 \pm 0.636$	$10.305 \pm 1.667$	$15.18 \pm 2.698$	5
	GN	50	$0.11 \pm 0.0219$	$1.958 \pm 0.534$	$14.785 \pm 1.052$	$23.59 \pm 1.859$	6
		100	$0.357 \pm 0.081$	$5.987 \pm 1.091$	$52.349 \pm 4.253$	$86.21 \pm 3.471$	7
	SAPN	50	$0.089 \pm 0.0311$	$2.479 \pm 0.7433$	$15.116 \pm 1.475$	$20.151 \pm 1.619$	8
		100	$0.323 \pm 0.07$	$6.308 \pm 1.366$	$53.397 \pm 4.253$	$77.456 \pm 4.474$	9
CIFAR-10		50	$0.056 \pm 0.023$	$0.915 \pm 0.934$	$0.338 \pm 0.325$	$0.892 \pm 0.402$	10
	OH	100	$0.061 \pm 0.04$	$0.769 \pm 0.461$	$0.451 \pm 0.41$	$0.648 \pm 0.407$	11
	TI	50	$0.082 \pm 0.037$	$0.928 \pm 0.815$	$0.388 \pm 0.243$	$0.423 \pm 0.362$	12
	11	100	$0.056 \pm 0.048$	$0.992 \pm 0.517$	$0.469 \pm 0.426$	$0.415 \pm 0.232$	13
	SVHN	50	$0.055 \pm 0.032$	$0.948 \pm 0.699$	$0.665 \pm 0.565$	$0.414 \pm 0.357$	14
		100	$0.075 \pm 0.036$	$1.291 \pm 0.925$	$0.736 \pm 0.658$	$0.581 \pm 0.343$	15
	GN	50	$0.107 \pm 0.083$	$1.344 \pm 1.156$	$1.708 \pm 0.421$	$3.001 \pm 0.696$	16
		100	$0.127 \pm 0.087$	$1.531 \pm 0.767$	$5.855 \pm 0.552$	$8.703 \pm 0.926$	17
	SAPN	50	$0.1146 \pm 0.044$	$1.854 \pm 0.894$	$2.299 \pm 0.691$	$2.561 \pm 0.762$	18
		100	$0.208 \pm 0.05$	$5.502 \pm 1.156$	$8.225 \pm 0.866$	$9.554 \pm 0.489$	19
FashionMNIST	ОН	50	$0.02 \pm 0.012$	$0.34 \pm 0.162$	$0.669 \pm 0.566$	$0.575 \pm 0.423$	20
		100	$0.059 \pm 0.032$	$0.801 \pm 0.402$	$0.305 \pm 0.237$	$0.774 \pm 0.343$	21
	FP	50	$0.105 \pm 0.0526$	$2.168 \pm 0.774$	$7.263 \pm 0.622$	$5.305 \pm 0.405$	22
		100	$0.195 \pm 0.0457$	$4.819 \pm 1.077$	$9.056 \pm 0.462$	$11.286 \pm 0.751$	23
	TI	50	$0.04 \pm 0.03$	$0.798 \pm 0.542$	$0.897 \pm 0.516$	$0.897 \pm 0.516$	24
		100	$0.065 \pm 0.03$	$1.66 \pm 0.45$	$1.4 \pm 0.488$	$1.912 \pm 0.683$	25
	GN	50	$0.047 \pm 0.03$	$0.533 \pm 0.347$	$2.819 \pm 0.703$	$3.843 \pm 0.704$	26
		100	$0.074 \pm 0.041$	$1.325 \pm 0.631$	$9.042 \pm 0.699$	$15.511 \pm 0.445$	27
_	SAPN	50	$0.036 \pm 0.022$	$0.52 \pm 0.303$	$2.799 \pm 0.497$	$2.799 \pm 0.497$	28
		100	$0.076 \pm 0.044$	$1.411 \pm 0.548$	$8.464 \pm 0.553$	$8.464 \pm 0.553$	29

TABLE IV CORRELATION RESULTS FOR THE DISSIMILARITY MEASURES BETWEEN  $S_l$  AND  $S_u$  WITH OOD CONTAMINATION AND SSDL ACCURACY.

$S_1$	$\mathbf{n}_{\mathbf{l}}$	$d_{\ell_1}$	$d_{\ell_2}$	$d_{JS}$	$d_{\mathbf{C}}$
	60	-0.876	-0.898	-0.969	-0.944
MNIST	100	-0.805	-0.83	-0.786	-0.948
	150	-0.794	-0.822	-0.81	-0.944
	60	-0.823	-0.853	-0.944	-0.921
CIFAR-10	100	-0.826	-0.878	-0.966	-0.947
	150	-0.808	-0.838	-0.952	-0.927
	60	-0.2	-0.268	-0.735	-0.789
FashionMNIST	100	-0.264	-0.326	-0.781	-0.824
	150	-0.286	-0.347	-0.785	-0.827

density based distances present more confidence. We suspect that this is related to the quantitative approximation of the feature distribution mismatch implemented both in the  $d_{\rm JS}$  and  $d_{\rm C}$  distances. In Table II we indicate the distance-based preference ranking in parentheses. The OOD configurations resulting in the best SSDL accuracy are contained in the top two selections seven out of nine times. Note that with our proposed approach we can do this selection *before* SSDL training and thus improve the overall result.

# VI. CONCLUSIONS AND RECOMMENDATIONS

In this work we extensively tested the behavior of the MixMatch algorithm under various OOD unlabelled data settings. We introduced a set of quantitative data selection heuristics, DeDiMs, to rank unlabelled datasets *ante hoc* according to their expected benefit to SSDL. Our results lead us to the following conclusions and recommendations:

 Real-world usage scenarios of SSDL can include different degrees of OOD data contamination in the unlabelled dataset Su: for instance, with a deep learning model trained for medical imaging analysis, unlabelled data can include images within the same domain, but capturing different pathologies not present in the labelled data. A close scenario has been simulated with the OH setting which resulted in a subtle accuracy degradation in most cases. However, the accuracy gain obtained vis-a-vis the

- fully supervised baseline is still substantial, making the application of SSDL attractive in such a setting.
- Another plausible real-world scenario for SSDL is the inclusion of widely available unlabelled datasets, e.g., built with web crawlers, where the domain shift can be more substantial. This scenario has been simulated with the OOD types similar and different. We can observe that notions of semantic similarity between labelled and unlabelled dataset pairings, e.g., (MNIST-SVHN) or (FashionMNIST-FP), do not necessarily imply an SSDL accuracy gain. The quantitative comparison of the density function plots in Table I suggest a higher similarity for dataset pairs with less semantic similarity, for some of the tested dataset setups. Distance measures, in particular  $d_C$ , seem to be an accurate and systematic proxy for SSDL accuracy, according to our test results. This is visible when comparing the accuracy and distance results of the previous pairings to (MNIST-TI) and (FashionMNIST-TI) which have higher accuracies and, also, surprisingly, lower distance measurements. We speculate how this can be related to the quality of the feature extractor that the usage of more diverse data can yield, as the positive results often yielded with self-supervised learning [44].
- Overall, according to the results yielded in this work, the implemented DeDiMs correlate strongly with the yielded SSDL accuracy. In particular density based measures yielded high correlation indices with the MixMatch accuracy. This suggests that this approach can be applied in SSDL prior to learning, aiding the unlabelled data selection process and mitigate the class distribution mismatch problem. The facts that they are agnostic, simple and fast to compute make them particularly suitable for practical application in SSDL. Different OOD detectors [48] use the feature space for building a discrimination criteria to filter OOD data. Our results suggest that online OOD data filtering approaches for SSDL as the ones developed in [27], [10] might benefit from using the

- feature space for OOD detection. Other criteria for online OOD detection during training as the model Softmax output used in [27] might discard data that might be useful for learning. We plan to test this in future work.
- The proposed DeDiMs are very efficient to implement, with only the calculation to a set of small samples, with no need of training a deep learning model, as a pretrained feature extractor using ImageNet is used. Using an ImageNet pre-trained model to calculate the feature densities demnostrated to suffice to quantify unlabelledto-labelled dataset affinity, with no need of fine-tuning the model using the target dataset. As suggested, our method can be used to rank different unlabelled datasets. Preliminar studies show a growing concern in the carbon footprint of training deep learning models [2]. Our method is cheap and does not need additional model training. Moreover, it can also be extended to filter OOD data as a previous step before training, avoiding the need of increasing the computational cost at each epoch, as seen in [27] for instance. Either as a dataset ranking method or a OOD data filtering, our method can be considered to be cheap as no model training is needed.
- The usage of the proposed DeDiMs to assess the impact of using an unlabelled dataset  $S_u$  over another, shifts the attention to data-oriented approaches to improve the model performance. We argue that data quality measurements for deep learning is often an overlooked topic within the community. For instance in [26], the authors propose a method to estimate how good a labelled dataset can be for training a deep learning model, measuring the dataset sparsity through the usage of different clustering algorithms. In real-world applications, using one model over another one with an assumed better performance according to previous reports, might no yield statistically significant performance gains, as the dataset used in the first place might not be appropriate. Our proposed method in this work, extends the work in citemendez2019using, to the context of SSDL, and proposes a metric to select an unlabelled dataset  $S_u$ .
- The claim done in [47] regarding the impact of close to boundary OOD data compared to far to boundary OOD data, relies on an Euclidean space projection of the data, which might not be very convenient for complex image data. In this work, we have gathered evidence about how Euclidean based comparison distances correlate worse to the density function based approaches tested. Using a density based divergence like the tested Jensen-Shannon divergence might not correlate well with semantic similarity, but according to our tests explains better the obtained SSDL accuracy. Using such divergence definition, close to boundary OOD data yields better SSDL accuracy. This shows how the feature extractor and the consequent feature space projections play a more important role in the final model performance than the original input space, as the feature space is built through non-linear convolutional operations that significantly changes it.
- Exploring the impact of OOD data in other aspects of SSDL performance, namely robustness, explainability and

- confidence can be important also, as recommended in [29]. As seen in [9], the usage of SSDL can also improve other model properties such as uncertainty. Therefore, evaluating the impact of distribution mismatch between  $S_l$  and  $S_u$ can be very useful. For instance, in [3] the impact of OOD data is tested in the overall model robustness and explainability. Moreover, a quantitative approach to OOD data can help to better estimate and test the impact of OOD data into other model performance aspects.
- Unsupervised domain adaptation is a challenge where the test data (target domain) presents a different distribution than the training data (source domain). Using SSDL for such setting can leverage unlabelled data in the target domain. For instance, in [46], an SSDL approach is proposed for unsupervised domain adaptation. Quantifying the degrees of OOD for the unlabelled data can improve the analysis of the test results and estimate the performance for unsupervised domain adaptation.
- Finally, the proposed test bed and distance measures can be used for a more systematic quantitative evaluation of SSDL algorithms. Counter-intuitively, datasets with a high perceived semantic similarity can be less challenging than other more dissimilar unlabelled datasets. Furthermore, this finding leads us to speculate about the actual mismatch between features learned by an artificial neural network and humans, adding more evidence to consider when studying the relationship between artificial and biological learning systems.

In future work, we plan to extend the test bed to other SSDL variants, depth-first analyses (e.g., fewer tasks with more training epochs), additional axes of test bed variables (e.g.,  $n_u$ ) and more testing around the appropriate dissimilarity measures parameters. We consider that investigating the relationship between generic feature similarity and SSDL downstream performance further is an appealing topic. The fact that feature dissimilarity scores can be calculated before SSDL training and independent of the SSDL model offers an interesting profile for application. Here connections to OOD detection [48], concept drift [42] and class distribution mismatch [11] would also be interesting to explore. Efficient and effective quantitative dataset evaluation prior training a deep learning is indeed an appealing topic to develop, this in the context of pushing the envelope further in computational efficient deep learning solutions, and narrowing the gap between deep learning research and its real-world application.

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